



NUMERICAL EXPLORATION OF MHD NON-NEWTONIAN NANOFLUID FLOW PAST A BIDIRECTIONAL SURFACE WITH RADIATION AND JOULE'S HEAT

T. Jayachandra Reddy¹, B. Ramoorthy Reddy², A. Mohanarami Reddy³

¹Dept. of Mathematics, Sri Venkateswara College of Engineering, Tirupati-517507, A.P., India.

Email: jayachandradevity@svce.edu.in

²Department of H&S, Mother Theresa Institute of Engineering Technology, Palamaner-517408, A.P., India.

Email: ramoorthymaths@gmail.com

³Dept. of Mathematics, Sri Venkateswara College of Engineering and Technology, Chittoor-517127, A.P., India.

Abstract:

The present study examines the stimulus of a magnetic field on the three-dimensional movement of Casson nanofluid over a stretchable surface embedded in a porous medium. The belongings of various constraints on the fluid dynamics are also analyzed. The governing nonlinear partial differential equations representing the fluid flow problem are converted into dimensionless ordinary differential equations using similarity transformations. These resulting ODEs are then solved numerically using the R. K. based Shooting method. The impact of various parameters on the flow profiles is illustrated through graphical representations. It is observed that the velocity profile decreases with an increase in the magnetic field number. Moreover, greater radiation parameter values lead to a rise in the distribution of heat and the corresponding layer thickness.

Keywords: Heat and mass transfer, non-Newtonian fluid, MHD, radiation, first order chemical reaction

1. Introduction:

A non-Newtonian fluid is a fluid whose viscosity (resistance to flow) changes depending on the rate of shear strain, or the relative motion between its fluid layers. This behavior contrasts with Newtonian fluids, which maintain a constant viscosity regardless of the shear rate. Non-Newtonian fluids, such as Eyring–Powell fluid, Casson fluid, Prandtl fluid, Reiner–Philipp off fluid, Prandtl–Eyring fluid, Carreau fluid, micropolar fluid, and power-law fluid, have attracted considerable attention from researchers due to their wide range of applications in various industries. Among these, Casson fluid stands out as the most relevant. This fluid is vital in industries like food processing, adhesive and paint manufacturing, nuclear power plant cooling systems, and polymer production. Ali *et al.* (2019) investigated the motion of Casson nanofluid over an elastic sheet. Mabood *et al.* (2020) examined the flow of Casson nanofluid over a flexible surface. Gubena and Ibrahim (2023) studied the flow of Casson nanofluid on an expanding sheet, incorporating a heat flux model. A numerical scrutinization of MHD micropolar fluid flow due to stretching of variable thickened surface in the attendance of dissipation was reported by Kumar *et al.* (2019). The influence Eckert number on MHD micropolar fluid over a bending surface with uneven heat source/sink was reported by Kumar *et al.* (2019) and found an enhancement in fluid temperature for swelling values of non-uniform heat source/sink parameters.

In recent years, the analysis of hydromagnetic flow involving heat and mass transfer in porous medium has attracted the attention of many scholars because of its possible applications in diverse fields of science and technology such as - soil sciences, astrophysics, geophysics, nuclear power reactors, etc. In geophysics, it finds its applications in the design of MHD generators and accelerators, underground water energy storage systems etc. It is worth - mentioning that MHD is now undergoing a stage of great enlargement and differentiation of subject matter. These new problems draw the attention of the researchers due to their varied significance, in liquid metals, electrolytes ionized gases etc. Maleque *et al.* (2005) analyzed the impact of variable properties and Hall current on steady MHD laminar convective fluid flow over a porous rotating disk. Singh (2007) investigated steady MHD free convection and mass transfer flow, incorporating Hall current, viscous dissipation, Joule heating, and the effect of thermal diffusion. Devi *et al.* (2011) explored pulsating convective MHD flow with Hall current, a heat source, and viscous dissipation along a vertical porous plate. Singh *et al.* (2005) examined hydromagnetic free convection and mass transfer flow influenced by Joule heating, thermal diffusion, a heat source, and Hall current. Kumar *et al.* (2024) studied the behavior of nanofluids flowing over a stretchable sheet under the influence of convection.

Radiation plays a crucial role in many physical phenomena and has significant effects on various processes. Heat energy is transferred through fluid particles via radiation, which is a critical factor in engineering and numerous industrial applications, such as high-temperature operations in fuel pumps, paper plate manufacturing, frozen metal shards, and electronic chips. Consequently, scientists are compelled to study the radiation process, especially when driven by substantial temperature gradients. Researchers have explored radiation effects using diverse flow characteristics. Ahmad *et al.* (2024) investigated the thermal performance of fluid flow through a porous medium, incorporating thermal radiation within a channel between two walls. Albalawi *et al.* (2024) analyzed heat transfer in nanofluid motion around a cylinder, considering the impact of thermal radiation. Ramadevi *et al.* (2019) deliberated the influence of uneven heat source/sink and thermic heat on hybrid nanofluid flow over a bidirectional surface. Aslam *et al.* (2024) studied the effects of thermal radiation on fluid motion within permeable enclosures. Kumar *et al.* (2019) examined the role of heat sink/source on non-Newtonian fluid flow over a wedge. Kempannagari *et al.* (2020) researched the impact of Joule heating on fluid flow over an exponentially stretching sheet.

Chemical reactions play a crucial role in mass and heat transfer studies across academic and technology-driven fields due to their extensive industrial applications. They are essential in processes such as polymer synthesis, designing chemical processing equipment, cooling towers, fog formation, pollution control, dispersion, temperature regulation, and fiber insulation, among others. In industrial chemical operations, raw materials are intentionally subjected to chemical reactions, transforming inexpensive starting materials into high-quality, advanced products. Sandeep *et al.* (2012) have investigated the effect of radiation chemical reaction on transient MHD free convection flow over a vertical plate through a porous medium. Ramadevi *et al.* (2020) have found out the chemical effects on a steady MHD-free convection fluid past a stretched sheet with heat absorption by using the modified heat flux model. Kumar *et al.* (2023) made a study on free convection in MHD nanofluid flow with Heat source. Recently, Rathore *et al.* (2024) examined the flow and heat transfer features of nanofluid flow past a stretching sheet in the presence of radiation.

The literature survey reveals that the combined effects of chemical reactions and electrically conductive MHD have not been extensively studied. This research focuses on the impact of Joule heating, magnetic fields, radiation, heat sources/sinks, and chemical reactions on the three-dimensional flow of Casson nanofluid over a rotating, stretching surface in the presence of porous media. By analyzing how chemical reactions influence flow dynamics, scientists and engineers can enhance the efficiency of heat and mass transfer processes and design systems with optimized flow characteristics. The governing partial differential equations (PDEs) are transformed into dimensionless ordinary differential equations (ODEs) using similarity variables. These ODEs are then solved numerically using the RKF-45 method. The effects of various dimensionless parameters on temperature, velocity, and concentration profiles are illustrated through graphical representations.

2. Formulation:

Let us ponder a steady, 3D, incompressible non-Newtonian nanofluid model subject to borderline conditions from initial to free stream velocity. The classical is electrically conductive, and the exterior is stretchable and penetrable. The velocity of the stretchable surface is $u_w = ax$, here a is the stretching constant. The velocity components are considered as (u, v, w) along (x, y, z) directions. The momentum equation has electric outcome is calculated in the directions of x -axis and y -axis, as shown in Fig. 1. The temperature distribution is dominated by thermal radiation and heat generation/absorption. The occurrence of higher-order chemical reactions is also considered.

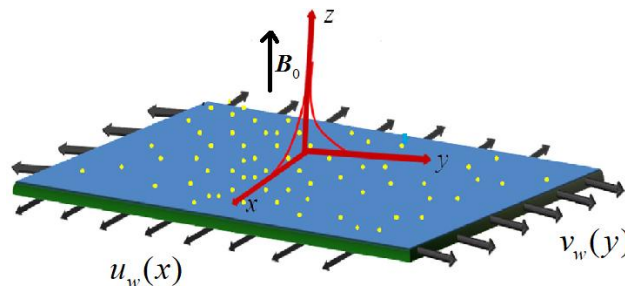


Fig. 1: Geometry of flow problem.

The governing equations are:

$$\frac{\partial v}{\partial y} + \frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0 \quad (1)$$

$$u \frac{\partial u}{\partial x} + w \frac{\partial u}{\partial z} + v \frac{\partial u}{\partial y} = \nu_{nf} \left(1 + \frac{1}{\beta} \right) \frac{\partial^2 u}{\partial z^2} - \frac{\nu_{nf}}{K^*} u - \frac{\sigma_{nf}}{\rho_{nf}} \beta_0^2 u \quad (2)$$

$$u \frac{\partial v}{\partial x} + w \frac{\partial v}{\partial z} + v \frac{\partial v}{\partial y} = \nu_{nf} \left(1 + \frac{1}{\beta} \right) \frac{\partial^2 v}{\partial z^2} - \frac{\nu_{nf}}{K^*} v - \frac{\sigma_{nf}}{\rho_{nf}} \beta_0^2 v \quad (3)$$

$$u \frac{\partial T}{\partial x} + w \frac{\partial T}{\partial z} + v \frac{\partial T}{\partial y} = \alpha_{nf} \frac{\partial^2 T}{\partial z^2} + \frac{\sigma_{nf}}{(\rho C_p)_{nf}} [(u+v)\beta_0]^2 + \frac{Q_0}{(\rho C_p)_{nf}} (T - T_\infty) - \frac{1}{(\rho C_p)_{nf}} \frac{\partial q_r}{\partial z} \quad (4)$$

$$u \frac{\partial C}{\partial x} + w \frac{\partial C}{\partial z} + v \frac{\partial C}{\partial y} = D \frac{\partial^2 C}{\partial z^2} - K_n (C - C_\infty) \quad (5)$$

The subjected boundary conditions are

$$\left. \begin{aligned} u = u_w = ax, v = 0, -k_{nf} \frac{\partial T}{\partial z} = h_f (T_f - T), C \rightarrow C_w, w = 0, \quad \text{at } z = 0 \\ w \rightarrow 0, u \rightarrow 0, v \rightarrow 0, T \rightarrow T_\infty, C \rightarrow C_\infty \quad \text{as } z \rightarrow \infty \end{aligned} \right\} \quad (6)$$

The Rosseland approximation is applied for radiative heat flux as,

$$q_r = -\frac{4\sigma^*}{3K^*} \frac{\partial T^4}{\partial z} \quad (7)$$

Here, the Stefan-Boltzman constant is σ^* and the mean absorption coefficient is expressed as k^* .

Consider the similarity transformations

$$\xi = \sqrt{\frac{a}{\nu_f}} z, u = axF'(\xi), v = axg(\xi), w = -(a\nu_f)^{1/2} F(\xi), T = T_\infty [1 + (\varepsilon - 1)\theta(\xi)] \quad (8)$$

The temperature ratio parameter is $\varepsilon = T_f / T_\infty$.

The nanofluid terms are

$$\begin{aligned} \mu_{nf} = \frac{\mu_f}{(1-\phi)^{2.5}}, \rho_{nf} = (1-\phi)\rho_f + \phi\rho_s, (\rho C_p)_{nf} = (1-\phi)(\rho C_p)_f + \phi(\rho C_p)_s, \sigma = \frac{\sigma_s}{\sigma_f}, \\ \sigma_{nf} = \sigma_f \left[1 + \frac{3(\sigma-1)\phi}{(\sigma+2) - (\sigma-1)\phi} \right], k_{nf} = k_f \left[\frac{k_s + 2k_f - 2\phi(k_f - k_s)}{k_s + 2k_f + \phi(k_f - k_s)} \right], \alpha_{nf} = \frac{k_{nf}}{(\rho C_p)_{nf}}. \end{aligned} \quad (9)$$

Utilizing equation (8), the equations (2) – (6) becomes,

$$\Phi_2 \left(1 + \frac{1}{\beta} \right) F''' + \Phi_1 \left(-F_1 F'^2 + FF'' - F'^2 \right) + \Phi_3 Ha^2 F' - \Phi_2 K_1 F' = 0 \quad (10)$$

$$\Phi_2 \left(1 + \frac{1}{\beta} \right) g'' - \Phi_1 \left(F'g - Fg' - F_1 g \right) + \Phi_3 Ha^2 g' - \Phi_2 K_1 g = 0 \quad (11)$$

$$\begin{aligned} \frac{1}{Pr} \left\{ \Phi_5 \theta'' + 4Ra \left[1 + \theta(\varepsilon - 1)^2 \right] (\varepsilon - 1) \theta'^2 + \frac{4}{3} Ra (1 + \theta(\varepsilon - 1))^3 \theta'' \right\} + \\ \left[\Phi_4 F \theta' + Ha^2 Ec \Phi_3 [(F' + g)]^2 \right] + \delta \theta = 0 \end{aligned} \quad (12)$$

$$\frac{1}{Sc} \phi'' + \phi' F - \gamma \phi = 0 \quad (13)$$

The associated non-dimensional borderlines are

$$\left. \begin{aligned} F(\xi) = 0, F'(\xi) = 1, -\Phi_5 \theta'(\xi) = Bi(1 - \theta(\xi)), g(\xi) = 0, \phi(\xi) = 1, \text{ at } \xi = 0 \\ F'(\xi) \rightarrow 0, g(\xi) \rightarrow 0, \theta(\xi) \rightarrow 0, \phi(\xi) \rightarrow 0 \end{aligned} \right\} \text{ as } \xi \rightarrow \infty \quad (14)$$

Here

$$\Phi_1 = (1 - \phi) + \phi(\rho_s / \rho_f), \Phi_2 = (1 - \phi)^{-2.5}, \Phi_3 = 1 + \frac{3(\sigma - 1)\phi}{(\sigma + 2) - (\sigma - 1)\phi}, \Phi_4 = (1 - \phi) + \phi \frac{(\rho c_p)_s}{(\rho c_p)_f}, \Phi_5 = \frac{k_{nf}}{k_f},$$

Here $K_1 = \frac{\nu_f}{K^* a}$ is the porous parameter, $Ha^2 = \frac{\sigma_f B_0^2}{a \rho_f}$ the magnetic parameter, $Ra = \frac{4\sigma^* T_\infty^3}{k_f k^*}$ the radiation

parameter, $Pr = \frac{(\mu C_p)_f}{k_f}$ is the Prandtl number, $Ec = \frac{a^2 x^2}{(C_p)_f (T_f - T_\infty)}$ is the Eckert number, $\delta = \frac{Q_0}{a(\rho C_p)_f}$

is the heat generation/absorption parameter, and $Bi = \frac{h_f}{k_f} \sqrt{\frac{\nu_f}{a}}$ is the Biot number is $Bi = \frac{h_f}{k_f} \sqrt{\frac{\nu_f}{a}}$.

The physical quantities are obtained as follows,

The non-dimensional skin friction coefficients (C_{fx}, C_{fy}) , local Nusselt number (Nu_x) and Sherwood numbers are:

$$\left. \begin{aligned} C_{fx} (Re_x)^{1/2} = A_2 \left(1 + \frac{1}{\beta} \right) F''(0), C_{fy} (Re_x)^{1/2} = A_2 \left(1 + \frac{1}{\beta} \right) g'(0), \\ Nu_x (Re_x)^{-1/2} = - \left[\Phi_5 + \frac{4}{3} Ra \{ 1 + (\varepsilon - 1) \theta(0) \}^3 \right] \theta'(0), Sh_x (Re_x)^{-1/2} = -\phi'(0), \end{aligned} \right\} \quad (15)$$

Here $Re_x = \frac{x u_w}{\nu_f}$ stands for local Reynolds number.

3. Results and Discussion:

This section details the computational methodology. Equations (10)-(14) demonstrate both nonlinearity and interdependence. By utilizing similarity transformations, the partial differential governing equations are converted into nonlinear algebraic equations. These transformed equations are subsequently substituted into the system for further analysis. It is thus recommended to address these equations through a numerical technique. Numerical solutions for the boundary value problem (BVP) must be obtained using the RKF-45 method algorithm. Initially, to accomplish this objective, transform the BVP into an initial value problem (IVP) with specified starting conditions. The physical clarification of each dimensionless parameters in momentum (F'), energy (θ) and concentration (ϕ) are focused by fixing other constraints and assign to them some fixed input values such as $Ha = 2, n = 1, K_1 = 1, F_1 = 0.2, Ra = 0.3, \delta = 0.3, \beta = 0.2, \gamma = 0.1, Bi = 1.5, Ec = 1, Pr = 7, Sc = 1.2, \Phi_1 = 0.6, \Phi_2 = 0.6, \Phi_4 = 0.4, \Phi_5 = 0.4$. The thermo physical values of the base fluid and nanoparticle are shown in Table 1.

Table 1: The thermo physical properties are

	$\rho (kgm^{-1})$	$k (Wm^{-1}K^{-1})$	$C_p (Jkg^{-1}K^{-1})$	$\sigma (Sm^{-1})$
Base fluid	1060	0.505	8933	1.07×10^{-4}
$MnFe_2O_4$	4870	0.67	130	120×10^6

Figs. 2-4 display the geometrical representation of magnetic constraints for larger values on $F'(\xi), \theta(\xi) \& \phi(\xi)$. A noteworthy reduction in these outlines is detected with a higher slope gradient variation. This is due to the consequence of drag force in the porous medium. It is detected from Fig. 3 and 4, that the energy and concentration distribution is boosted for higher magnetic parameter values. Fig. 5 portrays

the consequence of Ra on $\theta(\xi)$. Graphs reveal that intensification in radiation parameter enhances the temperature distribution.

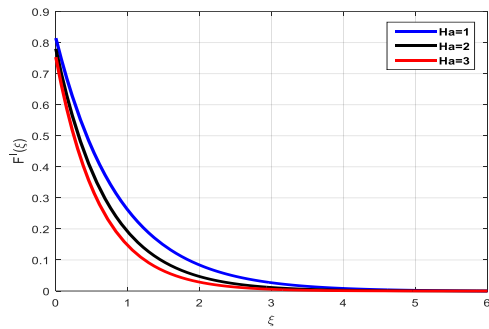


Fig. 2. Stimulus of Ha on $F'(\xi)$.

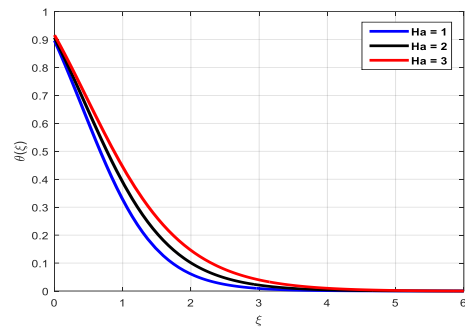


Fig. 3. Stimulus of Ha on $\theta(\xi)$

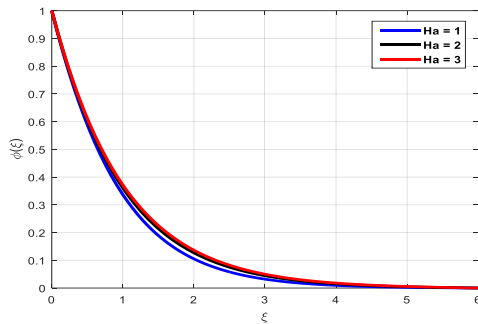


Fig. 4. Stimulus of Ha on $\phi(\xi)$

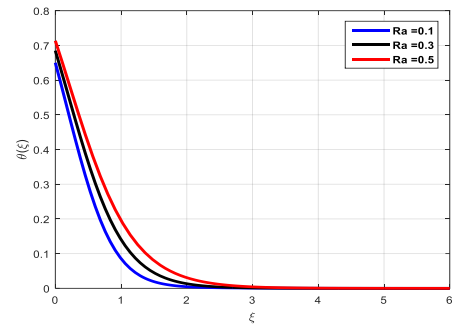


Fig. 5. Stimulus of Ra on $\theta(\xi)$

Fig. 6 is sketched to evaluate the performance of the nature of the porosity parameter on the velocity. The increase in K_1 declines the $F'(\xi)$. The reason behind this is magnetic strength and porous medium. The effect of δ on the distribution of heat is depicted in Fig. 7. The rise in δ intensifies the curves of heat. The heat movement within the system will accelerate as heat source levels climb. The heat sink will function as an exchanger, transferring heat from the external environment into the nanofluid.

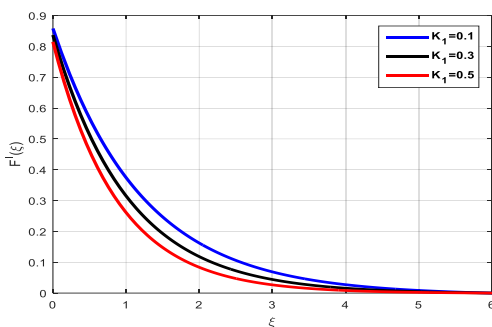


Fig. 6. Stimulus of K_1 on $F'(\xi)$

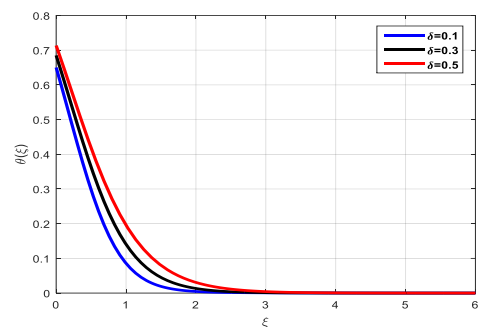
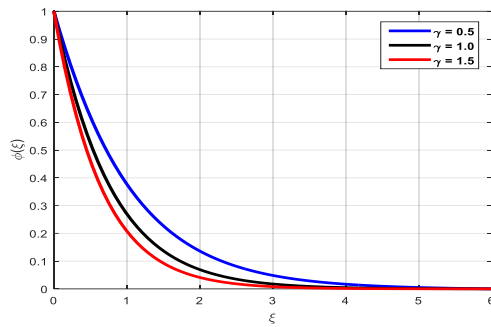
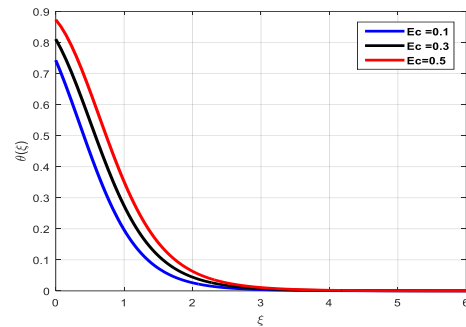
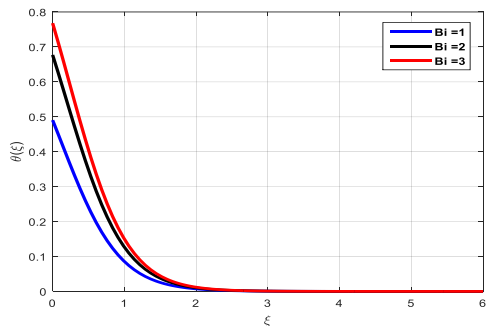
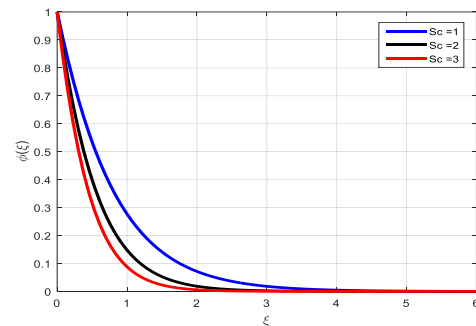


Fig. 7. Stimulus of δ on $\theta(\xi)$

The effect of γ on the heat is depicted in Fig. 8. The disparities lead to a decay in the $\phi(\xi)$ for more values of chemical reaction parameter. The nano-fluid particles in the strained surface are the purpose for the decline of species gradient in the permeable medium. The impact of Eckert number is sketched in Fig. 9 to encounter temperature distribution. Automatic energy is derived from thermal energy in energy distribution pertaining to viscous dissipation. It is noted that augmenting Ec less forces acted in the viscous dissipation of temperature distribution. Due to impact of heat generation dominations led Eckert's number to enhance to higher values.


Fig. 8. Stimulus of γ on $\theta(\xi)$

Fig. 9. Stimulus of Ec on $\theta(\xi)$

The impact of Biot number is sketched in Fig. 10 to encounter temperature distribution. It is noted that augmenting Bi causes an enactment in the temperature distribution. Figure 11 is portrayed to analyse the impact of Schmidt number (Sc) on concentration. By increasing values of Schmidt number decreases the fluid concentration. Actually, Schmidt number is the ratio of momentum diffusivity and mass diffusivity. Hence, the distribution of concentration and the corresponding layer thickness decreases for increasing values of Schmidt number.


Fig. 10. Stimulus of Bi on $\theta(\xi)$

Fig. 11. Stimulus of Sc on $\phi(\xi)$

4. Conclusions

A steady, three-dimensional magnetohydrodynamic flow of Casson fluid over a stretching sheet is studied in the presence of a porous medium. With the aid of appropriate similarity variables, the governing PDEs are transformed into ODEs which are solved numerically using the RKF method. The following is a list of some of the study's key findings based on the above mentioned results and discussion:

- A decrease in the distribution of velocity is detected for increasing values of magnetic field and porosity parameter.
- Concentration profile falls for growing value of Schmidt number and chemical reaction constraint.
- Temperature is a swelling factor of radiation and variable heat source/sink constraints.
- It is perceived that increasing values of solutal slip parameter reduces the distribution of concentration.
- The improvement in the distribution of heat can be seen as the Biot number upsurges.

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