PERFORMANCE OF A STATIONARY SAVONIUS ROTOR WITH CIRCULAR ARC BLADE PROFILE

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Abstract: Static torque and drag coefficients of a stationary Savonius rotor with circular arc blade profile have been investigated by measuring the pressure distribution on the blade surfaces for different rotor angles. Experiments have been performed at a Reynolds Number \(1.8 \times 10^5\) with rotors having no overlap. Results indicate that static torque coefficients vary considerably with the rotor angle.

Keywords: Savonius rotor, blade profile, drag coefficient.

INTRODUCTION

The Savonius rotor has been subject of interest since the 1930’s and has been studied extensively. It is a vertical axis wind turbine and has a lower efficiency as compared to other vertical axis wind turbines such as Darrieus Rotor. Nevertheless, it is used as an alternative to wind power extraction because of its simple design and good starting torque at low wind speeds\(^1,5,10,13\). Rigorous studies on the performance characteristics of the Savonius rotor are found in the literatures and these enable the identification of an optimum geometrical configuration for practical design\(^2,4,6,9,11\). However, only a few studies are reported in the literatures which give information regarding the total aerodynamic load on the structure and mechanism of the rotation of the rotor. This paper attempts an experimental study on the aerodynamic load on a stationary Savonius rotor with different multiple number of blades.

EXPERIMENTAL SETUP AND PROCEDURE

The objectives of the investigation of wind loading on the circular arc bladed Savonius rotor have been realized essentially with the help of a subsonic wind tunnel experimental set up of the Savonius rotor and an inclined manometer bank. The schematic diagram of the wind tunnel is shown in Figure 1.

The wind tunnel

The open circuit subsonic wind tunnel was 6.55m (21.5ft) long with a test section of \((49\text{cm} \times 49\text{cm})\) cross-section. Figure 1 depicts the wind tunnel used for the experiment. The successive sections of the wind tunnel comprised of converging mouth entry, perspex section, rectangular section, fan section (two rotary axial flow fans), butterfly section, silencer with honeycomb section, an eddy breaker, diverging section, converging section, 2 ft long rectangular section, 1 ft long flow straightened section, 2 ft long rectangular exit section. The central longitudinal axis of the wind tunnel was maintained at a constant height from the floor.

The rotor

The Savonius rotor was made up of three blades of diameter, \(d = 72.75\text{ mm}\) and height, \(H = 300\text{ mm}\). The blades were made of PVC material. The whole rotor was fixed on an iron frame by using two side shafts and two ball bearings. The pressure measurements were done at 12 pressure tappings on each blade. The tappings were made with copper tubes of 1.5mm outer diameter and 10mm length which were press fitted to the tapping holes. The tappings were located at the mid-plane of one side of each blade, so that pressure distribution at every 10° on the blade surface could be measured. The pressure tappings were connected to an inclined multi-manometer (manometric fluid was water and had an accuracy of \(\pm 0.1\text{ mm of water column}\)) through 2mm PVC tubes. The pressures were measured at every 10° interval of rotor angle (Figure 3.5), so that a detailed picture of the aerodynamic loading and torque characteristics could be obtained.

AERODYNAMIC CHARACTERISTICS CALCULATION

The flow pattern produced by the rotor blades is characterized by complicated floe phenomenon such as high turbulence, unsteadiness and flow separation\(^1,6,11,14\). The combined effect of these floe features in turn produces pressure differences between the front and back surfaces of the blades. These pressure differences result in the calculation of the aerodynamic forces from numerical integrations. Pressure coefficient is defined as

\[
C_p = \frac{P - P_0}{\frac{1}{2} \rho U_0^2}
\]

where, \(P - P_0\) = Difference between blade and atmospheric pressure in Pascal,
\[ \rho = \text{Density of air} = 1.2 \text{ kg/m}^3, \]
\[ U_0 = \text{Free stream velocity} = 13 \text{ m/s}. \]

Figure 1. The Wind tunnel

For Savonius rotor, at a particular rotor angle, \( \alpha \) the rotor blades experience forces (per unit span length) due to pressure difference between the concave surface and convex surface and these forces can be resolved into two components, \( F_n \) and \( F_t \). Since the blade surfaces are circular, \( F_n \) and \( F_t \) pass through the center of the circle. The drag coefficients in normal and tangential directions can be written as follows

\[
C_n = \frac{F_n}{\frac{1}{2} \rho U_0^2 d}
\]
\[
C_t = \frac{F_t}{\frac{1}{2} \rho U_0^2 d}
\]

To obtain the drag coefficients in the normal and tangential directions of the chord, the values of \( F_n \) and \( F_t \) must be known beforehand. The values of the forces \( F_n \) and \( F_t \) are obtained by integrating the pressure for a blade as follows

\[
F_n = \int_0^\pi \Delta p_2 \frac{d}{2} \cos \phi d\phi = \sum_{i=1}^{12} \Delta p_i \frac{d}{2} \cos \phi_i \Delta \phi_i
\]

and similarly,

\[
F_t = \sum_{i=1}^{12} \Delta p_i \frac{d}{2} \sin \phi_i \Delta \phi_i
\]

where, \( \Delta p_i \) is the difference in pressure on the concave and convex surfaces at a particular pressure tapping, i. This \( \Delta p_i \) is multiplied by the differential area \( \frac{d}{2} \cdot 1.1 \) \( d\phi \) considering unit height of the blade to obtain the value of differential tangential and normal forces. Then numerical integration is carried out for the whole diameter of each blade corresponding to the limit 0 to \( \pi \) for obtaining the value of \( F_n \) and \( F_t \). The force \( F_n \) is responsible for producing a torque on the shaft of the rotor and this torque coefficient for a single blade at a particular rotor angle can be written as

\[
C_q(\alpha) = C_n(\alpha) \times \frac{1-s}{2-s}
\]

The total static torque coefficient produced on the rotor shaft by the three blades can be expressed as follows

\[
C_q(\alpha) = [C_n(\alpha) + C_n(\alpha + 120^\circ) + C_n(\alpha + 240^\circ)] \times \frac{1-s}{(2-s)^2}
\]

where,

\( C_n(\alpha), C_n(\alpha + 120^\circ) \) and \( C_n(\alpha + 240^\circ) \) refer to the drag coefficients of the first, second and third blades respectively at rotor angle \( \alpha \).

RESULTS AND DISCUSSIONS

Normal drag coefficient, \( C_n \) for an individual blade is shown in Fig. 2 for different rotor angles. For the first blade, normal drag coefficient \( C_n(\alpha) \) increases with the increase of rotor angle from \( \alpha = 0^\circ \) to \( 40^\circ \), and then drag coefficient decreases with the increase of the rotor angle \( \alpha \), up to \( 90^\circ \). The drag coefficient \( C_n(\alpha) \) for the first blade which is responsible for the torque production is positive for a rotor angle of \( 0^\circ \) to \( 80^\circ \) and reaches its maximum value at \( \alpha = 40^\circ \). At \( \alpha = 90^\circ \) the value becomes negative. The drag coefficient \( C_n(\alpha + 120^\circ) \), for the second blade, is higher compared to that of the first blade. Drag coefficient \( C_n(\alpha + 120^\circ) \), for the second blade is always positive, i.e. is in favor of torque production from \( \alpha = 0^\circ \) to \( 110^\circ \). The drag coefficient \( C_n(\alpha + 240^\circ) \), decreases in the negative values with the increase of rotor angle.

Tangential drag coefficient, \( C_t \) with individual blade effect is shown in Fig. 3 for different rotor angles. For the first blade, tangential drag coefficient, \( C_t(\alpha) \) increases with the increase of rotor angle from \( \alpha = 0^\circ \) to \( 40^\circ \) and then decreases up to \( 90^\circ \). The drag coefficient, \( C_t(\alpha) \) for the first blade which is responsible for thrust production on the support of the rotor, is positive for the rotor angle of \( 0^\circ \) to \( 90^\circ \) and reaches its maximum value at \( \alpha = 40^\circ \). At \( \alpha = 90^\circ \) becomes slightly negative. The drag coefficient \( C_t(\alpha + 120^\circ) \), for the second blade, is higher compared to that of the first blade. Drag coefficient \( C_t(\alpha + 120^\circ) \) for the second blade is positive, i.e. it is in favor of thrust production from \( 0^\circ \) to \( 110^\circ \) angle of rotation. The drag coefficient \( C_t(\alpha + 240^\circ) \), for the third blade,
decreases in the negative value from $\alpha = 240^\circ$ to $\alpha = 360^\circ$ with the increase of rotor angle. So, it produces negative thrust from $\alpha = 240^\circ$ to $\alpha = 360^\circ$.

Total static torque coefficient at different rotor angles is shown in Fig. 4. The nature of this curve is exactly similar to the normal drag coefficient, $C_n$, with combined effect of three blades. Only difference is that the value of torque coefficient is greater than normal drag coefficient with combined blade effect. Here, the total static torque increases with the increase of the rotor angle up to $30^\circ$ and reaches its maximum value and then decreases to a negative value at $\alpha = 90^\circ$. The curve repeats from $120^\circ$ to $230^\circ$ and again from $240^\circ$ to $350^\circ$ angle of rotation.

![Figure 2. Normal drag coefficient of individual blade effect](image1)

![Figure 3. Tangential drag coefficient of individual blade effect](image2)
Figure 4. Total static torque coefficient at different rotor angles

NOMENCLATURE

- $a$: Overlap distance
- $C_p$: Pressure coefficient
- $C_{pb}$: Pressure coefficient for concave surface of the blade
- $C_{px}$: Pressure coefficient for convex surface of the blade
- $C_t$: Drag coefficient in the transverse direction of the chord
- $C_n$: Drag coefficient in the normal direction of the chord
- $C_q$: Static torque coefficient for a single blade
- $C_Q$: Total static torque coefficient
- $d$: Diameter of blade
- $D$: Diameter of the rotor
- $F_n$: Normal forces acting on a blade
- $F_t$: Tangential forces acting on a blade
- $H$: Height of the rotor
- $\Delta h_w$: Specific weight of manometer liquid
- $P$: Pressure on blade
- $\Delta p$: Difference of pressure between concave and convex surfaces of a blade
- $P_a$: Atmospheric pressure
- $Re$: Reynolds number
- $S$: Ratio of overlap distance to diameter of blade
- $T$: Static torque on a blade
- $U_0$: Free stream velocity
- $V_r$: Relative velocity
- $V_w$: Component of relative velocity along $U_0$
- $\alpha$: Rotor angle
- $\phi$: Angle of pressure tappings
- $\lambda$: Tip speed ratio, $D\omega/2U_0$
- $\omega$: Angular speed of the rotor
- $\nu$: Kinematic viscosity of air
CONCLUSION
The total static torque coefficients for the rotor at different rotor angles are analyzed. From the results obtained the following conclusions can be drawn for a stationary savonious rotor with circular arc blade profile.

i. The normal drag coefficient for individual blade increases gradually from 0° and it becomes the maximum at around 150° angle of rotation. After 240° angle of rotation it becomes negative up to 350°.

ii. However, tangential drag coefficient for individual blade becomes the maximum at around 130° angle of rotation and up to 240° its value remains positive. Again, after 260° angle of rotation the value becomes negative.

iii. The total torque coefficient becomes the maximum at 30°, 150° and 260° positions and the variation is more or less cyclic which is evident from the experimental values.

REFERENCES