

# A Comparative Study of Pricing Option with Efficient Methods

Sujon Chandra Sutradhar and A B M Shahadat Hossain

**Abstract**— Our main objective of this paper is to introduce four individual techniques of pricing options; the techniques are Binomial method, Trinomial method, Monte Carlo simulation and Black-Scholes-Merton model. Because they play a significant role in option valuation of stock price dynamics, risk managements as well as stock market. In this paper, we briefly discuss all these four methods with their properties and behavior. We also focused on numerical technique for the higher accuracy of option pricing and compare them graphically. We use the Computer Algebra System (CAS) Python (Edition 2019.3.1) for this purpose.

**Index Terms**— Binomial method, Trinomial method, Monte Carlo simulation, Black-Scholes-Merton model.

## I. INTRODUCTION

PRICING option is very popular now a day and many scholars have attracted to work in valuing option by using of the tree methods. Black and Scholes (1973) introduced the well-known pricing option model. As the intelligence of mathematics and analysis behind this model is very deep and critical to realize and that is the reason is not well known by the universal readers. Merton published a renowned paper named ‘Theory of rational option pricing’. There gained a great achievement and makes a great breakthrough in the area of option pricing when they introduced the model named ‘BLS formula or Black Scholes Merton.’ Later Cox et al. introduced a binomial option-valuation model which is widely realized and easy to assent due to its momentary mathematical methods and the imbedded economic significance. So, it is broadly used in the financial market. This model is very much simple and allows only two possible paths in a certain time interval. The underlying stocks can go upward and go downward as well with a probability. Though it is easy

to use, it has some drawback also. It could lead major error in the calculations especially when the option is more complex. So it should not be the right choice for more complicated options. Then an amazing Trinomial option pricing model was introduced by Boyle. [1] Later it was modified and well solved by Boyle with Lau, Kamrad and Ritchen. They have proposed that there are three different paths for the underlying assets which is up, equal and down for each time interval with a certain probability. It is more realistic than the binomial option pricing and can used in the more complicated options. It is now widely used in different fields of finance.

Later Han developed trinomial tree model. He developed an efficient way of valuing option numerically and described the results for continuous distribution of underlying stock price movements and found more accurate results compared to the binomial option pricing model.

In the field of finance, Monte Carlo option pricing model is very much popular now a day. In an MC option model, Monte Carlo approaches is used to compute the value of an option with multiple sources of improbability or with complicated features. In 1977, Phelim Boyle first introduce the Monte Carlo model for pricing European options. In 1996, M. Broadie and P. Glasserman worked on pricing Asian option using Monte Carlo simulation. An important development of Monte Carlo methods for options early exercise features were introduced in 1996 by Carriere.

Our focus in this paper is to price option by using binomial and trinomial option pricing method. For practical view, we use the market data so that we can predict the market volatility from the previous data, which is known as the historical volatility. We work for both European and American call option pricing. We also compare the option value with the exact solution BLS option-pricing model and MC option pricing method for the European option. Again, we also discuss the dividend effect for option pricing and show the results in graphical representation

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## II. METHODOLOGY

### A. Option

Options are derivatives, which are dealt both on exchanges and in the over-the-counter market. It is

contract that gives rights to the holder but not obligation. There are mainly two categories of options.

- Call option
- Put option

Call is one type of these options which gives its holder the right but not the obligation to buy an underlying asset in a specific price on a specific date. Similarly put is another type of option that gives right but not obligation to its owner to sell an underlying asset in a specific price on a specific date. The predetermined price and date are known as strike price ( $K$ ) and expiration date ( $T$ ) respectively. If the option is exercised before the expiration date then it is American option [2] otherwise if the option is exercised only on the expiration date then it is the European option. Let

$S_T$  be the final price and  $K$  be the strike price of the underlying asset. Let us consider that the option costs nothing.

In a call option, payoff from long position is,  $\max(S_T - K, 0)$ . This replicates that if  $S_T > K$  the option will be exercised and will not be exercised if  $S_T \leq K$ . The payoff to its holder from a long position

in a put option is  $\max(K - S_T, 0)$ . The Payoff from short position in a call option is,

$$-\max(S_T - K, 0) = \min(K - S_T, 0)$$

In a long positioned put option the payoff for its holder is  $\max(K - S_T, 0)$

In European option, we can only exercise our option on the expiration date but in American type option, we can exercise it before the determined date, because of it, this type of option is more costly than the previous type.

#### B. Binomial option pricing model (BOPM)

In BOPM the whole time frame divided into small interval of size  $\delta t$ . It confirms us that in each time period the stock price moves either up  $Su$  and down  $Sd$  from its initial value  $S$ . In fig. 1 we have showed a two steps binomial tree.

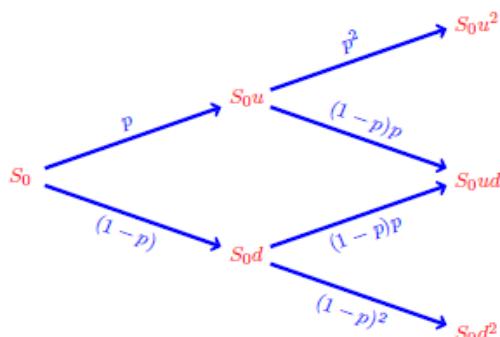


Fig. 1. Two steps binomial tree.

Where  $u > 1$  and  $d < 1$ . The movement from  $S$  to  $Su$  is called the up movement and  $Sd$  is called the down movement. The probability for the up movement as well as for the down movement is  $p$  and  $(1-p)$  respectively. During the time interval  $\delta t$ , the parameters  $p, u, d$  must give the correct value for the mean and the variance. The expected return from an asset in the risk neutral world is the risk-free interest rate and it is denoted by  $r$ . When there is yield of  $q$ , then the expected return from the underlying asset will be  $(r-q)$ . This means that the expected value after certain time interval of size  $\delta t$  must be  $Se^{(r-q)\delta t}$ . [3] If we match the mean return with the above mentioned tree, we get the following relationship

$$\begin{aligned} Se^{(r-q)\delta t} &= pSu + (1-p)Sd \\ \Rightarrow e^{(r-q)\delta t} &= pu + (1-p)d \end{aligned} \quad (1)$$

The variance of a variable  $x$  is defined by  $E(x^2) - [E(x)]^2$ . Now let us define  $R$  is the percentage change of the asset price at time  $\delta t$ , there is probability  $p$  that  $(1+R)$  is  $u$  and a probability  $(1-p)$  is  $d$ , then the variance of  $(1+R)$  is  $pu^2 + (1-p)d^2 - e^{2(r-q)\delta t}$ . The variance of  $(1+R)$  is the same as the variance of  $R$  and this is  $\sigma^2\delta t$ .

$$So \quad pu^2 + (1-p)d^2 - e^{2(r-q)\delta t} = \sigma^2\delta t \quad (2)$$

From equation (1)

$$\begin{aligned} e^{(r-q)\delta t}(u+d) &= pu^2 + (1-p)d^2 + ud \text{ so} \\ e^{(r-q)\delta t}(u+d) - ud - e^{2(r-q)\delta t} &= \sigma^2\delta t \end{aligned} \quad (3)$$

A last but not least condition applied by CRR (1979) consider  $ud = 1$ , and by solving the above equation we can find the relation, [4]

$$p = \frac{a-d}{u-d}, \quad u = e^{\sigma\sqrt{\delta t}}, \quad d = e^{-\sigma\sqrt{\delta t}}, \quad a = e^{(r-q)\delta t}$$

#### C. Expressing the approach algebraically

Assume the life of the option is partitioned into  $n$  subinterval of length  $\delta t$ . We will mention to the  $j^{th}$  node at time  $i\delta t$  as the  $(i, j)$  node, (where  $0 \leq i \leq n$  and  $0 \leq j \leq i$ ). Define  $f_{i,j}$  is the option value at the  $(i, j)$  node. At the  $(i, j)$  node the underlying asset is  $S_0u^i d^{i-j}$ . For a call option payoff

from the underlying asset at time  $T$  (at the maturity) is  $\max(S_T - K, 0)$ . So

$$f_{n,j} = \max(S_0 u^j d^{n-j} - K, 0); j = 0, 1, \dots, n$$

Similarly, for a put option payoff at time  $T$  is  $\max(K - S_T, 0)$ ; so,

$$f_{n,j} = \max(K - S_0 u^j d^{n-j}, 0); j = 0, 1, \dots, n$$

The probability of moving at time  $i\delta t$  from node  $(i, j)$  to the  $(i+1, j+1)$  node at time  $(i+1)\delta t$  is  $p_u$ , and similarly the probability of moving at time  $i\delta t$  from node  $(i, j)$  to the  $(i+1, j)$  node at time  $(i+1)\delta t$  is  $(1-p)$ . If early exercise is not allowed, then risk neutral valuation gives

$$f_{i,j} = e^{-r\delta t} [ p f_{i+1,j+1} + (1-p) f_{i+1,j} ]$$

For  $0 \leq i \leq n-1$  and  $0 \leq j \leq i$ . Now if we consider early exercise such as American option, then we should compare  $f_{i,j}$  with the options intrinsic value, so, for a call option, [5]

$$f_{i,j} = \max \left\{ S_0 u^j d^{i-j} - K, e^{-r\delta t} [ p f_{i+1,j+1} + (1-p) f_{i+1,j} ] \right\}$$

And for put option,

$$f_{i,j} = \max \left\{ K - S_0 u^j d^{i-j}, e^{-r\delta t} [ p f_{i+1,j+1} + (1-p) f_{i+1,j} ] \right\}$$

#### D. Trinomial option pricing model (TOPM)

The calculating procedure of TOPM is as similar as the BOPM. Although it is more realistic. In trinomial tree, we observed three possibilities of the movement of share price (stock price)  $S_u$ ,  $S_d$  and  $S_m$  from the initial stock price  $S$ . The probabilities of this movements are  $p_u$ ,  $p_m$  and  $p_d$ .

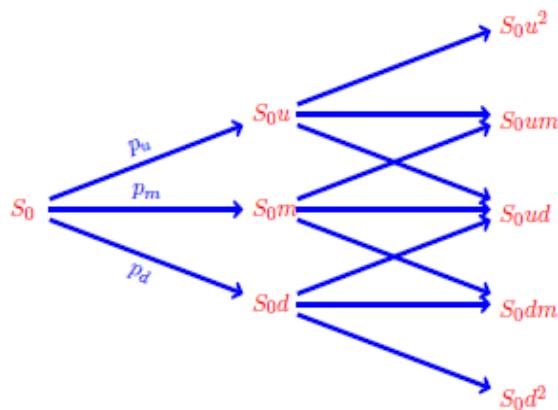


Fig.2. Two steps trinomial tree

In our model, if we claim stock price increases from step  $(n-1)$  to step  $n$ , then the stock price at step

$(n+1)$  is  $uS_n$ ,  $mS_n$  and  $dS_n$  with the probability  $p_u$ ,  $p_m$  and  $p_d$  respectively. We have showed simple two steps trinomial tree in the above fig. 2

In the risk neutral condition, the expected asset price after the first interval is  $S_0 e^{r\delta t}$  where ( $\delta t = T/n$ ); that is,

$$\begin{aligned} S_0 e^{r\delta t} &= p_u S_0 u + p_m S_0 m + p_d S_0 d \\ \Rightarrow e^{r\delta t} &= up_u + mp_m + dp_d \end{aligned} \quad (4)$$

Another two conditions come from the variance and property of probabilities;

$$u^2 p_u + m^2 p_m + d^2 p_d - (e^{r\delta t})^2 = \sigma^2 \delta t \quad (5)$$

$$p_u + p_m + p_d = 1 \quad (6)$$

By solving the above equations (4), (5), and (6) we find the probabilities;

$$\begin{aligned} p_u &= \left( \frac{e^{r\delta t/2} - e^{-\sigma\sqrt{\delta t/2}}}{e^{\sigma\sqrt{\delta t/2}} - e^{-\sigma\sqrt{\delta t/2}}} \right); p_d = \left( \frac{e^{\sigma\sqrt{\delta t/2}} - e^{r\delta t/2}}{e^{\sigma\sqrt{\delta t/2}} - e^{-\sigma\sqrt{\delta t/2}}} \right); \\ p_m &= 1 - p_u - p_d; \end{aligned}$$

Where,  $u = e^{\sigma\sqrt{2\delta t}}$ ,  $d = e^{-\sigma\sqrt{2\delta t}}$  and  $m = 1$ .

The methodology of pricing option using a trinomial tree (TT) is same as the binomial tree (BT), once the share price tree is built and the option payoff at maturity time  $T$  are calculated. For the call option  $\max(S_T - K, 0)$  and for the put option  $\max(K - S_T, 0)$ . After that it remains to apply the following backward induction algorithm, where  $i$  represents the time position and the  $j$  represents the space position, then

$$C_{i,j} = e^{-r\delta t} [ p_u C_{i+1,j+1} + p_m C_{i+1,j} + p_d C_{i+1,j-1} ]$$

Now if the option is the American type then the option can be exercised before the expiry date ( $T$ ) with the same strike price, then the backward recursion takes the following form; [6]

For call:

$$C_{i,j} = \max \left( S_{i,j} - K, e^{-r\delta t} [ p_u C_{i+1,j+1} + p_m C_{i+1,j} + p_d C_{i+1,j-1} ] \right)$$

For put:

$$C_{i,j} = \max \left( K - S_{i,j}, e^{-r\delta t} [ p_u C_{i+1,j+1} + p_m C_{i+1,j} + p_d C_{i+1,j-1} ] \right)$$

#### E. Monte Carlo Simulation

The stochastic differential equation with drift term  $\mu$  and diffusion term  $\sigma$  is  $dS_t = \mu S_t dt + \sigma S_t dW_t$  where,  $W_t$  is a standard Brownian process. Now if the

drift and diffusion are correlated with both  $S$  and  $t$  then discrete approximation is  $\Delta S = \mu S \delta t + \sigma S \varepsilon \Delta W$  where  $\varepsilon \sim \mathcal{N}(0,1)$ . Now using Itô's lemma  $d \ln(S_t) = (\mu - \sigma^2/2) dt + \sigma dW_t$ . Here  $\ln(S_t)$

follows a standardized wiener process with constant mean and variance. This means that the change of  $\ln(S_t)$  within time interval  $\delta t$  is normally distributed. [7] i.e

$$\begin{aligned} \ln(S_{t+\delta t}) - \ln(S_t) &\sim \mathcal{N}\left[\left(\mu - \frac{\sigma^2}{2}\right)\delta t, \sigma^2 \delta t\right] \\ \text{or, } \ln(S_{t+\delta t}) &\sim \mathcal{N}\left[\ln(S_t) + \left(\mu - \frac{\sigma^2}{2}\right)\delta t, \sigma^2 \delta t\right] \\ \ln(S_{t+\delta t}) - \ln(S_t) &= \left(\mu - \frac{\sigma^2}{2}\right)\delta t + \sigma \varepsilon \sqrt{\delta t} \\ \text{or, } S_{t+\delta t} &= S_t \exp\left[\left(\mu - \frac{\sigma^2}{2}\right)\delta t + \sigma \varepsilon \sqrt{\delta t}\right] \end{aligned}$$

If  $t = 0$ , and  $\delta t = T$ , the equation moves to

$$S_T = S_0 \exp\left[\left(\mu - \frac{\sigma^2}{2}\right)T + \sigma \varepsilon \sqrt{T}\right] \quad (7)$$

MC simulation is broadly used in for the commodity pricing where the payoff depends on the previous prices of the underlying commodities. In order to price the option first we need to divide the maturity time  $T$  of options into  $n$  subintervals with length  $\delta t$ , then by using the equation (7) sample the possible random path for the stock price and get the stock price  $S_T$  at the maturity date. After collecting all the payoffs, discount the average payoff we get the expected results, which is

$$\text{For call: } e^{-rT} \left( \frac{1}{n} \sum_{i=1}^n \max(S_T - K, 0) \right)$$

$$\text{For put: } e^{-rT} \left( \frac{1}{n} \sum_{i=1}^n \max(K - S_T, 0) \right)$$

#### F. Black-Scholes Merton pricing formula

If the option value  $f$ , risk neutral interest rate  $r$ , market annual volatility  $\sigma$  and the stock price  $S$  then from the solution of BLS-Merton differential equation, [8][9]

$$\frac{\partial f}{\partial t} + rf \frac{\partial f}{\partial S} + \frac{1}{2} \sigma^2 S^2 \frac{\partial^2 f}{\partial S^2} = rf$$

Prices of the European call and put options form are  $C = S_0 N(d_1) - Ke^{-rT} N(d_2)$  (8)

$$P = Ke^{-rT} N(-d_2) - S_0 N(-d_1) \quad (9)$$

$$\text{Where } d_1 = \frac{\ln(S_0 / K) + (r + \sigma^2 / 2)(T - t)}{\sigma \sqrt{T - t}};$$

$$d_2 = \frac{\ln(S_0 / K) + (r - \sigma^2 / 2)(T - t)}{\sigma \sqrt{T - t}};$$

The formula  $N(x)$  is the CDF for a standard normal distribution with mean 0 and variance 1. [10]

### III. RESULT

TABLE I  
AMERICAN CALL OPTION PRICING UNDER TWO DIFFERENT METHODS

Variable	Value	Binomial Tree	Trinomial Tree
Interest Rate	0.01	155.5790	155.3498
	0.02	158.3135	158.0743
	0.03	161.0505	160.8033
	0.04	163.7898	163.5365
	0.05	166.5308	166.2733
Volatility (%)	18	150.6632	151.2171
	20	151.3778	152.3539
	23	155.5790	155.3499
	25	158.4847	158.0472
	30	165.7912	164.8304
Strike Price	785	155.5790	155.3498
	900	72.828	72.5624
	800	143.6316	143.1555
	700	234.2008	233.9966
	750	186.1183	186.8503
Maturity Time	100	155.570	155.3498
	200	171.8844	170.6728
	300	184.6971	182.7576
	400	195.6898	195.3513
	50	148.5626	148.7628

TABLE II

## EUROPEAN CALL OPTION PRICES UNDER DIFFERENT METHODS

Variable	Value	BT Model	TT Model	Black Scholes	Monte Carlo
Number of steps	5	155.5790	155.5161	155.5160	97.5437
	10	155.3499	155.6727	155.5161	195.1493
	100	155.4879	155.5219	155.5160	119.3861
	1000	155.5192	155.5160	155.5160	155.3216
	5000	155.5166	155.5161	155.5160	153.3974
Interest Rate	0.01	155.5790	155.5161	155.5160	153.3974
	0.02	158.3135	158.0743	158.2202	155.9964
	0.03	161.0505	160.8034	160.9311	157.5958
	0.05	166.5308	166.2733	166.3700	164.2374
	0.1	180.2500	179.9936	180.0392	178.0168
Volatility	23%	155.5790	155.5161	155.5160	153.3974
	30%	165.7912	164.8304	164.1484	162.6272
	35%	173.1325	171.6475	171.5658	169.9201
	20%	151.3778	152.3579	152.7103	150.5558
	15%	149.6079	149.5380	149.6437	146.6667
Strike Price	785	155.5790	155.5161	155.5160	153.3974
	900	72.828	72.5624	71.5205	69.6888
	800	143.6316	143.1555	142.7277	140.4281
	700	234.2008	233.9966	234.2826	232.4011
	750	186.1183	186.8503	186.87851	184.0479
Maturity Time	100	155.5790	155.5161	155.5160	153.3974
	200	171.8844	170.6728	170.1959	169.2282
	300	184.6971	182.7576	183.8515	181.1051
	400	195.6898	195.3513	196.3507	196.4881
	50	148.5626	148.7628	148.7374	145.8121

In this paper, we use the daily data of Google (NASDAQ: GOOG) from 2015-01' to '2017-07' and find the historical volatility 23%, we consider the initial stock price \$930.5, risk free interest rate 1% and 100 days maturity times, we consider the 252 trading days and zero dividend yield here. The results from the American call option is in table 1, and European call option price is in table 2

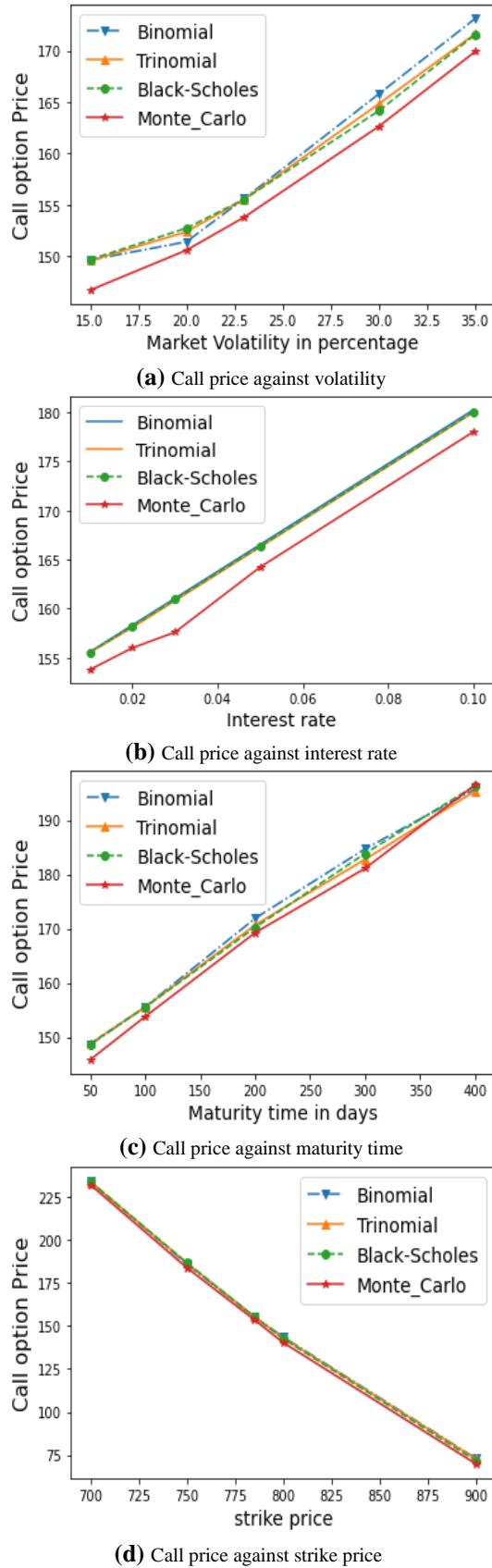
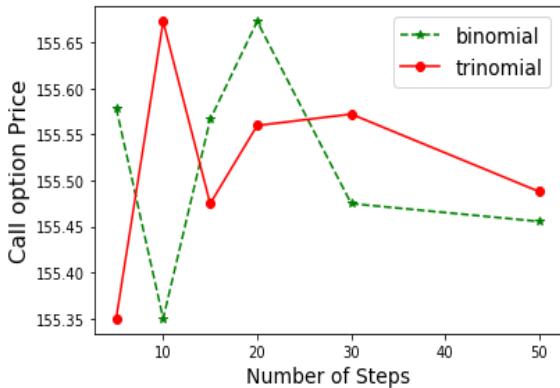
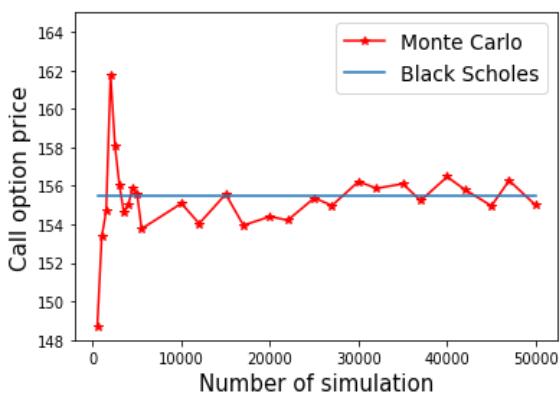


Fig. 3. European call option pricing under different volatility, interest rate, maturity, and strike price



(a) Call price against number of steps

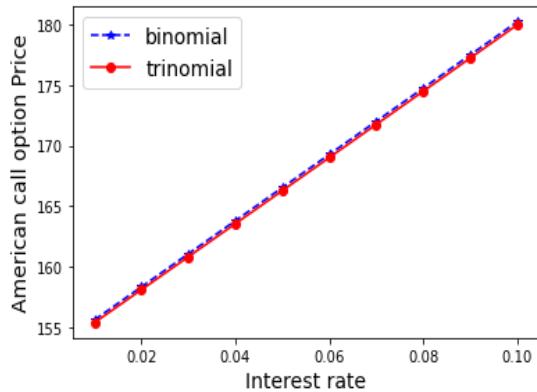


(b) Call price under Monte Carlo simulation

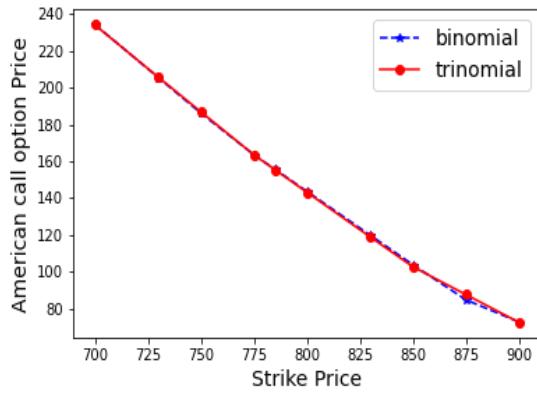
Fig. 4. European call Option Pricing under different step size and Monte Carlo simulation

In Fig. 3, we tried to show how the behavior of European call option value changes under different factors as volatility, interest rate, expiration time and strike prices with four different methods as binomial, trinomial, Monte Carlo and Black-Scholes model. In fig. 3(a). we see that the call option price increases with volatility. The four-mentioned methods almost give the same solution but trinomial method gives the result more similar to the exact solution, Black-Scholes model. In fig. 3(b). it is clear that call price increases with the interest rate. In this case, Monte Carlo simulation gives us a little fluctuating result than the others. In fig. 3(c). it is evident that call price increases with the increases of maturity time almost linearly. In fig. 3(d). it is obvious that call price decreases if we increase the strike price. In this case, we see that all the methods give almost exact result.

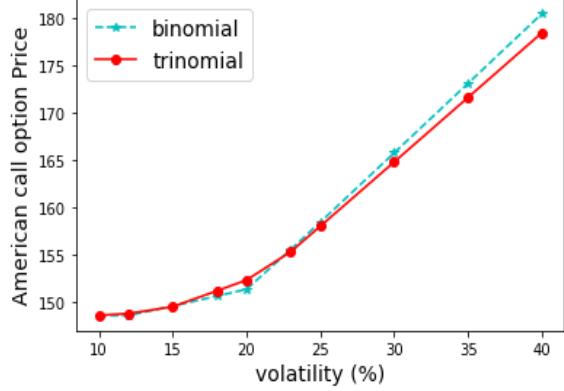
In Fig. 4, we tried to show how call option prices differ with the step sizes in both binomial and trinomial tree methods and how Monte Carlo simulation converges with Black-Scholes option prices by increasing number of simulations. In fig. 4(a). we find that, both binomial and trinomial tree give us almost same results with the increasing step sizes and in fig. 4(b) we established that if we increase the number of simulations Monte Carlo method converges the exact solution more quickly.



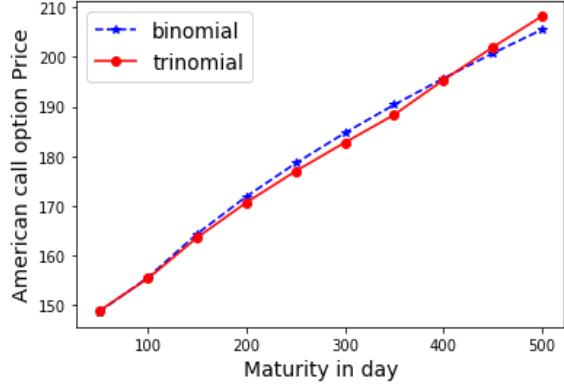
(a) American Call price against interest rate



(b) American Call price against strike price



(c) American Call price against volatility



(d) American Call price against maturity in day

Fig. 5. American Call options under binomial and trinomial methods.

Now it is time to discuss the option when it is the American type, and in Fig. 5, we show how call option prices differ with some essential factors as interest rates, strike prices, volatility and time to maturity under two essential option pricing methods such as binomial and trinomial tree method. In fig. 5(a). we can raise our opinion as by increasing interest rate, we can increase option value. In both methods, we almost get the same result. In fig. 5(b), it is clear that if we increase strike price, then option price decreases and both methods give the same result. Similarly, In fig. 5(c). we found that if the volatility increases or the market is more volatile then the value of American call option increases. Finally in fig. 5(d). when the maturity time is high then the option price is also high. So we can establish our opinion without any doubt that if our expiration time is high then it is obvious, the call option price is also high.

#### IV. CONCLUSION

In this paper we have discussed four effective option pricing methods, As the methods for put option pricing and call option pricing is almost same, we have discussed here only call option pricing here, we have used the market data and used historical volatility as the market volatility. All of the four methods give almost the same results, but we have noticed that the Monte Carlo simulation gives us best results when we use more simulations. We have also seen that by Monte Carlo simulation and Black Scholes model, we only price the European options, but with the binomial and trinomial method, we can value both the European and American type options and each case they give almost the same results.

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